# A STATISTICAL STUDY OF MAIN AND RESIDUAL ACCELERATIONS OF CORONAL MASS EJECTIONS 

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#### Abstract

In this paper we present the results of a statistical study of the accelerations of coronal mass ejections (CMEs). A CME usually undergoes a multiphased kinematic evolution, with a main acceleration phase characterized by a rapid increase of CME velocity in the inner corona, followed by a relatively smooth propagation phase characterized by a constant speed or a small residual acceleration in the outer corona. We study both the main acceleration and the residual acceleration for 50 CME events based on Large Angle Spectrometric Coronagraph (LASCO) observations. We find that the magnitude of the main acceleration has a wide distribution, from 2.8 to $4464.0 \mathrm{~m} \mathrm{~s}^{-2}$, with a median (average) value of $170.1\left(330.9 \mathrm{~m} \mathrm{~s}^{-2}\right)$, and a standard deviation of $644.8 \mathrm{~m} \mathrm{~s}^{-2}$, whereas the magnitude of the residual acceleration ranges only from -131.0 to $52.0 \mathrm{~m} \mathrm{~s}^{-2}$, with a median (average) value of $3.1\left(0.9 \mathrm{~m} \mathrm{~s}^{-2}\right)$ and a standard deviation of $25.3 \mathrm{~m} \mathrm{~s}^{-2}$. The duration of the main acceleration is also widely distributed, from 6 to 1200 minutes, with a median (average) value of 54 ( 180 minutes) and a standard deviation of 286 minutes.We find an intriguing scaling law between the acceleration magnitude $(A)$ and the acceleration duration $(T)$ over the entire parameter range of almost 3 orders of magnitude, which can be expressed as $A\left(\mathrm{~m} \mathrm{~s}^{-2}\right)=10,000 T^{-1}$ (minutes). The implications of these observational results on the issues of CME classification and CME modelings are discussed.


Subject headings: Sun: corona - Sun: coronal mass ejections (CMEs)

## 1. INTRODUCTION

Coronal mass ejections (CMEs) are a large-scale eruptive phenomenon that originate close to the Sun's surface and are accelerated in the Sun's inner corona. They propagate outward into the interplanetary space at a high speed and have a profound impact on the space environment throughout the heliosphere, including the geospace near the Earth. Since the first direct detection of CMEs in the early 1970s, more than 10,000 CMEs have been observed by various coronagraphs, both spaceborne and groundbased. In this paper we present a statistical study on the kinematic properties of CMEs, with a focus on CME's acceleration in the inner corona, which is relatively poorly known compared with the propagation properties of CMEs in the outer corona.

The kinematic properties of CMEs in the outer corona (e.g., $>2.0 R_{\odot}$ ) are well known from the observations of three major space-based white-light coronagraphs: Solwind (Howard et al. 1985), Solar Maximum Mission (SMM; Hundhausen et al. 1994), and Solar and Heliospheric Observatory (SOHO) LASCO (St. Cyr et al. 2000; Yashiro et al. 2004). It has been shown that the distribution of CME velocity in the outer corona ranges from about 50 to $3000 \mathrm{~km} \mathrm{~s}^{-1}$, with a single peak at about $300 \mathrm{~km} \mathrm{~s}^{-1}$. The median velocity in the distribution is about $350 \mathrm{~km} \mathrm{~s}^{-1}$, and the average velocity is about $400 \mathrm{~km} \mathrm{~s}^{-1}$. On the other hand, an individual CME usually exhibits a more or less constant speed in the outer corona. The distribution of the acceleration in the outer corona is always centered around the value of zero, with a narrow variation within about $\pm 30 \mathrm{~m} \mathrm{~s}^{-2}$ (Yashiro et al. 2004).

The relatively constant speed of CMEs in the outer corona indicates that CME acceleration takes place mainly in the inner corona, where strong but unstable magnetic field give rise to the eruption. Our earlier study based on several well-observed CME events showed that a CME's full kinematic evolution may un-

[^0]dergo three distinct phases: (1) an "initiation phase" of slow rise, (2) an "acceleration phase" of rapid velocity increase, and (3) finally a "propagation phase" with minor velocity variation (Zhang et al. 2001, 2004). The first two phases occur mainly in the inner corona (e.g., $<2.0 R_{\odot}$ or higher), while the third phase is largely in the outer corona (e.g., $>2.0 R_{\odot}$ ). CME acceleration measured during the acceleration phase in the inner corona is much different from that measured during the propagation phase in the outer corona. For the sake of clarity, we refer the former as main acceleration and the latter as residual acceleration hereafter. The same nomenclature has been used by Chen \& Krall (2003) in their theoretical modeling work on CME accelerations.

Observational studies have shown that the CME main acceleration in the inner corona manifests a great diversity, ranging from extremely impulsive evolution to extremely gradual evolution. Events with very strong acceleration (e.g., $>1000 \mathrm{~m} \mathrm{~s}^{-2}$ ) have been reported (Zhang et al. 2001; Alexander et al. 2002; Gallagher et al. 2003). On the other hand, there is a class of gradual CMEs characterized by very weak (e.g., $<20 \mathrm{~m} \mathrm{~s}^{-2}$ ) but persistent long-duration acceleration (e.g., lasting several hours) throughout both the inner and outer corona (Sheeley 1999; Sheeley et al. 1999; Srivastava et al. 1999, 2000). Recently, Zhang et al. (2004) reported a set of three CME events that showed impulsive, gradual, and intermediate acceleration. Most CME events reside between the extremely impulsive ones and the extremely gradual ones, characterized by acceleration on the order of hundreds of $\mathrm{m} \mathrm{s}^{-2}$, as seen in many events (Wood et al. 1999; Yurchyshyn 2002; Shanmugaraju et al. 2003; Qiu et al. 2004; Vršnak et al. 2004; Kundu et al. 2004; Sterling \& Moore 2005; Jing et al. 2005); note that erupting filaments are used as proxy to track the early acceleration of CME in some studies. St. Cyr et al. (1999) made a statistical study on CME acceleration using 46 CME features observed by ground-based Mauna Loa $K$-coronameter in the inner corona and with the SMM coronagraph in the outer corona. They found that the distribution of the acceleration ranged from -218 to $3270 \mathrm{~m} \mathrm{~s}^{-2}$, with a median (average) value of $44 \mathrm{~m} \mathrm{~s}^{-2}$
$\left(264 \mathrm{~m} \mathrm{~s}^{-2}\right)$. The appearance of negative numbers in the acceleration is due to the fact that they used second-order polynomial fitting to obtain the average acceleration over the entire height range observed; they did not distinguish the main acceleration from the residual acceleration in the fitting.

In this paper we present a statistical study of both the main and the residua accelerations of CMEs based on 50 events well observed by the three overlapping coronagraphs of SOHO LASCO. A preliminary and short result based on a small number of events has been reported earlier (Zhang 2005). The observations and event selection is presented in $\S 2$. In $\S 3$ we present two methods to calculate the main acceleration of CMEs: a direct method and an indirect flare-proxy method. A justification of the indirect method and discussion on CME-flare temporal relationship are included in $\S 3$. The results on statistical distributions of CME main accelerations (including both magnitude and duration) and residual accelerations, along with an intriguing finding of an acceleration scaling law, are given in $\S 4$. Discussions on the issues of CME classification and the implications on CME modelings are given in $\S 5$. Conclusions are presented in $\S 6$.

## 2. OBSERVATIONS AND DATA

The three LASCO coronagraphs, $\mathrm{C} 1, \mathrm{C} 2$, and C 3 , have complementary fields of view of $1.1-3.0,2-6$, and $4-30 R_{\odot}$, respectively (Brueckner et al. 1995). For a period of two and a half years (from the launch of SOHO in 1995 December to 1998 June), all three coronagraphs operated properly and provided full observations. Unfortunately, C1 failed after the half-year-long malfunction of the SOHO spacecraft during 1998. Therefore, this statistical study is limited to the early observations of LASCO, because C1 must be used to reveal CME acceleration in the inner corona. The simultaneous C2 and C3 observations showed CME evolution in the outer corona.

As in almost all CME studies, we use the leading edge (LE), the most outstanding and tractable feature of CME, to identify and measure CME heights in C 1 . The height-time measurements are subsequently used to calculate CME velocity and acceleration. The use of the LE in CME tracking is appropriate in this study, because it ensures a uniform tracking of the same feature when a CME travels across the C1, C2, and C3 fields of view. While C2 and C3 are typical broadband white-light coronagraphs that observe Thomson-scattered photospheric light scattered by electrons in the corona (the K corona), C 1 , on the other hand, is a spectroscopic coronagraph that observes the narrow emission lines from highly ionized ions in the corona (the E corona) as well as the K corona. The spectroscopic imaging capability of C 1 is achieved by using a Fabry-Perot interferometer that acts as a narrow-passband and tunable filter (passband of about $0.7 \AA$ ). C1 operated mainly in the following two strong coronal lines: the green line of Fe xiv at $5302 \AA$ (peak ionization temperature at $\sim 2.0 \mathrm{MK}$ ) and the red line of Fe x at $6376 \AA$ (peak ionization temperature at $\sim 1.0 \mathrm{MK}$ ). The C 1 observing mode was to cyclically take images through multiple points across the profile of one spectral line, and alternate for the two main lines. Because the strength of spectral lines depends on the ionization state of emitting elements, C 1 is sensitive to both temperature and density, whereas C 2 and C 3 are only sensitive to column density of electrons. As a result, the volume feature of CME seen in C1 often appeared much different from that of $\mathrm{C} 2 / \mathrm{C} 3$, which makes it difficult to track the internal features of CME across instruments. However, the LE of CME will be unambiguously identified in all three coronagraphs, because of its unique semicircular shape with enhanced brightness in the forefront and enveloping all other trailing features. To facilitate the
search, we have made heterogeneous running difference movies, which incorporate all C1 images taken in all wavelengths. By doing this, we are able to greatly enhance the search efficiency and maximize the search results.

C1 observations have a varying cadence depending on wavelength. For instance, on 1997 November 6, a typical 24 hr observing day, C 1 took 132 images in total, including 64 images at $5302.4 \AA$ (green line center), 15 images at $5302.7 \AA$, $24 \mathrm{im}-$ ages at $5309.2 \AA, 24$ images at $6376.4 \AA$ (red line center), and five images at $6380.9 \AA$. Taking into account the images in all wavelengths, C 1 had a cadence as short as 2 minutes to as long as 30 minutes. For any single wavelength, the cadence was 20 minutes at best. On the other hand, C2 and C3 had largely regular cadences, which were about 30 and 60 minutes, respectively; the cadences have been about twice as fast after the SOHO interruption in 1998.

By searching the C 1 image database of about 100,000 images in total, we found 74 CMEs seen in C 1 , and 50 of them are suitable to be used in this acceleration study. A C1 CME is found if the following two criteria are satisfied: (1) a CME LE, seen as a large-scale semicircular shape of enhanced brightness, clearly showed up in at least one C1 image, and (2) a CME appeared later in the C 2 field of view in a consistent position angle and at a consistent time indicating that the eruptive feature seen in C1 was indeed propagating into the C 2 field of view. We also found a large number of active features in C1 images; these features include large-scale dimmings and brightenings (often associated with fast CMEs), cavity lifting (often associated with slow CMEs), and loop arcades (posteruption features). However, most of these active events were not selected as C1 CMEs in this study, because their LEs, even present, were not clearly detected. We have documented all C 1 activities and the 74 C 1 CMEs in our C1 catalog. ${ }^{2}$ We excluded 24 C 1 CMEs from this study, mainly because we are not able to determine the duration of the main acceleration phase, e.g., only having 1 point of height-time measurement in the acceleration phase.

During the same C 1 observing period, LASCO C2 and C3 observed 1112 CMEs in total, listed in the CDAW (Coordinated Data Analysis Workshop) CME catalog generated and maintained by NASA and The Catholic University of America in cooperation with the Naval Research Laboratory. ${ }^{3}$ The much smaller number of CMEs seen in C 1 is mainly due to the fact that the background induced by the stray light is much higher in C 1 because of its approximation to the dominant photosphere. The low signal-to-noise ratio in C 1 images prevented most CMEs to be seen. In fact, most CMEs seen in C1 originated close to solar limb. The surface source regions were identified based on eruptive features, including large-scale dimmings and compact brightenings, seen by the Extreme-Ultraviolet Imaging Telescope (EIT, also on board SOHO ; Delaboudinière et al. 1995). Among the 50 events, 26 originated very close to the limb: all parts of the eruptive features seen in EIT were above the limb. And 19 events were from the front side, but close to the limb. The remaining five events originated from the backside of the Sun: eruptive features were seen in the EIT images neither on the disk nor above the limb. Compared to CMEs that originate close to the limb, a CME from the disk center is more difficult to detect in a coronagraph probably due to the following two effects. The first is the dilution effect: the disk-center CME has already traveled a certain distance, expanded, and hence weakened in brightness when

[^1]TABLE 1
Properties of the 50 CME Events Studied

| ID | Date | Time (UT) |  | $\mathrm{C} 1 / \mathrm{C} 2 / \mathrm{C} 3{ }^{\text {a }}$ | $\begin{gathered} \text { Source }^{\text {b }} \\ (\mathrm{deg}) \end{gathered}$ | Flare ${ }^{\text {c }}$ | Onset <br> (UT) | Peak <br> (UT) | $\begin{aligned} & \text { P.A. }{ }^{\mathrm{d}} \\ & (\mathrm{deg}) \end{aligned}$ | $\begin{aligned} & \mathrm{AW}^{\mathrm{e}} \\ & (\mathrm{deg}) \end{aligned}$ | $\operatorname{Velocity~(~} \mathrm{km} \mathrm{s}^{-1}$ ) |  | Acceleration Duration ${ }^{\text {h }}$ (minutes) | TY ${ }^{\text {i }}$ | Acceleration ( $\mathrm{m} \mathrm{s}^{-2}$ ) |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | C1 | C2 |  |  |  |  |  |  |  | Propogation ${ }^{\text {f }}$ | Final ${ }^{\text {g }}$ |  |  | Main ${ }^{\text {j }}$ | Residual ${ }^{\text {k }}$ |
| 1.... | 1996 Jun 17 | 02:03 | 02:23 | 2/3/3 | P080 | NA | NA | NA | 85 | 55 | 304.0 | 304.0 | 20 | DI | 253.3 | -3.9 |
| 2. | 1996 Jun 19 | 11:39 | 11:59 | 1/4/0 | N05E85 | B0.9 | 11:04 | 11:38 | 90 | 57 | 214.0 | 214.0 | 34 | FL | 104.9 | -12.8 |
|  | 1996 Jul 1 | 12:46 | 13:50 | 1/1/2 | P270 | B4.0 | 12:31 | 12:39 | 271 | 52 | 358.5 | 358.5 | 8 | FL | 746.9 | 35.3 |
|  | 1996 Oct 5 | 08:15 | 09:37 | 3/3/7 | P250 | A2.0 | 09:00 | 14:00 | 266 | 161 | 569.0 | 600.0 | 300 | DU | 33.3 | 16.8 |
|  | 1996 Oct 19 | 16:32 | 17:17 | 1/3/5 | S20E45 | B0.6 | 16:25 | 17:38 | 159 | 170 | 479.0 | 479.0 | 73 | FL | 109.4 | 9.4 |
| 6....... | 1996 Dec 23 | 11:13 | 13:28 | 1/0/11 | N05W85 | B1.5 | 10:43 | 10:53 | 284 | 68 | 263.0 | 262.4 | 10 | FL | 437.4 | 12.8 |
| 7....... | 1996 Dec 23 | 21:04 | 21:37 | 2/4/5 | S15W75 | B4.0 | 19:50 | 20:35 | 255 | 58 | 353.7 | 353.7 | 33 | DI | 178.6 | 4.6 |
| 8...... | 1996 Dec 24 | 13:20 | 13:28 | 2/4/4 | P270 | C2.1 | 13:03 | 13:11 | 265 | 69 | 324.4 | 324.4 | 8 | FL | 675.7 | -1.1 |
| 9...... | 1996 Dec 27 | 07:15 | 08:44 | 4/9/8 | NA | NA | NA | NA | 270 | 63 | 269.0 | 269.0 | 480 | DI | 9.3 | 6.8 |
| 10..... | 1997 Feb 23 | 00:15 | 02:55 | 4/2/4 | N25E80 | B7. 2 | 02:21 | 03:33 | 89 | 63 | 903.3 | 903.3 | 72 | DU | 209.1 | -4.3 |
| 11..... | 1997 Apr 4 | 05:51 | 06:57 | 4/12/14 | N40E80 | NA | NA | NA | 280 | 72 | 185.0 | 300.0 | 900 | DI | 5.6 | 3.1 |
| 12..... | 1997 Apr 9 | 11:55 | 12:06 | 1/3/6 | P225 | C1.5 | 10:00 | 11:40 | 277 | 63 | 484.3 | 484.3 | 50 | DI | 161.4 | 3.2 |
| 13..... | 1997 Apr 30 | 03:41 | 04:50 | 4/4/7 | P080 | A6.0 | 04:10 | 05:40 | 84 | 71 | 285.8 | 285.8 | 75 | DU | 63.5 | 0.4 |
| 14..... | 1997 May 18 | 09:01 | 23:13 | 8/3/5 | NA | NA | NA | NA | 88 | 32 | 352.9 | 510.0 | 700 | DI | 12.1 | 17.5 |
| 15..... | 1997 May 25 | 14:15 | 14:48 | 2/1/4 | S28E50 | B6.5 | 14:25 | 15:00 | 93 | 82 | 683.4 | 683.4 | 35 | FL | 325.4 | -2.4 |
| 16..... | 1997 May 27 | 09:35 | 10:15 | 1/3/6 | N02W80 | C4.6 | 09:31 | 09:57 | 271 | 47 | 428.1 | 428.1 | 26 | FL | 274.5 | 1.6 |
| 17..... | 1997 Jun 30 | 00:04 | 00:30 | 3/2/6 | N17W82 | C1.1 | 23:41 | 23:52 | 275 | 54 | 345.2 | 345.2 | 11 | FL | 523.0 | -0.4 |
| 18..... | 1997 Jul 8 | 14:13 | 16:09 | 3/3/0 | NA | NA | NA | NA | 279 | 54 | 75.3 | 100.0 | 480 | DI | 3.5 | 9.9 |
| 19..... | 1997 Jul 28 | 16:09 | 16:41 | 4/7/5 | P135 | NA | NA | NA | 99 | 77 | 167.4 | 220.0 | 40 | DI | 91.7 | -10.8 |
| 20..... | 1997 Sep 9 | 19:50 | 20:06 | 3/2/5 | P315 | NA | NA | NA | 284 | 101 | 726.0 | 800.0 | 30 | DI | 444.4 | -7.4 |
| 21..... | 1997 Sep 16 | 02:38 | 04:20 | 5/5/5 | P078 | NA | NA | NA | 78 | 72 | 251.4 | 350.0 | 360 | DI | 16.2 | 2.6 |
| 22.... | 1997 Sep 20 | 09:05 | 10:20 | 8/3/7 | P250 | C2.3 | 09:49 | 10:44 | 272 | 97 | 775.9 | 775.9 | 55 | DU | 235.1 | 5.0 |
| 23..... | 1997 Sep 28 | 08:03 | 08:40 | 7/4/12 | P060 | NA | NA | NA | 84 | 60 | 528.4 | 528.4 | 21 | DI | 419.4 | 5.5 |
| 24..... | 1997 Sep 29 | 14:34 | 15:46 | 3/3/7 | P045 | NA | NA | NA | 75 | 55 | 699.0 | 697.8 | 50 | DI | 232.6 | 11.6 |
| 25..... | 1997 Oct 6 | 10:13 | 10:31 | 3/2/10 | P225 | NA | NA | NA | 273 | 103 | 506.0 | 511.4 | 20 | DI | 426.1 | 3.6 |
| 26..... | 1997 Oct 12 | 05:59 | 06:26 | 2/2/5 | P225 | B2.3 | 06:02 | 06:54 | 258 | 62 | 777.6 | 777.6 | 52 | FL | 249.2 | -3.1 |
| 27..... | 1997 Oct 18 | 05:11 | 06:40 | 2/3/0 | P120 | NA | NA | NA | 96 | 50 | 234.5 | 380.0 | 180 | DI | 35.2 | 14.6 |
| 28..... | 1997 Oct 19 | 02:37 | 08:06 | 10/11/18 | P078 | NA | NA | NA | 89 | 63 | 131.8 | 390.0 | 1113 | DI | 5.8 | 6.1 |
| 29..... | 1997 Nov 6 | 11:54 | 12:08 | 2/1/4 | S18W63 | X9.4 | 11:49 | 11:55 | 266 | 360 | 1607.4 | 1607.4 | 6 | DU | 4464.9 | -131.0 |
| 30..... | 1997 Nov 14 | 08:30 | 10:14 | 3/2/4 | N21E70 | C4.6 | 09:05 | 10:36 | 79 | 86 | 1032.4 | 800.0 | 91 | DU | 146.5 | 39.6 |
| 31..... | 1997 Dec 9 | 11:49 | 12:55 | 3/3/2 | P225 | NA | NA | NA | 253 | 66 | 332.4 | 500.0 | 90 | DI | 92.6 | -12.5 |
| 32..... | 1997 Dec 14 | 00:57 | 02:03 | 1/1/5 | P135 | NA | NA | NA | 93 | 72 | 508.0 | 600.0 | 549 | DI | 18.5 | 9.5 |
| 33..... | 1998 Jan 2 | 23:17 | 23:28 | 2/6/7 | N22W38 | B6.4 | 23:25 | 02:25 | 296 | 360 | 397.3 | 397.3 | 170 | DU | 39.0 | 10.8 |
| 34..... | 1998 Jan 8 | 07:56 | 08:36 | 1/2/8 | S18E60 | B3.0 | 07:20 | 08:22 | 69 | 81 | 545.5 | 545.5 | 62 | FL | 146.6 | 1.7 |
| 35..... | 1998 Jan 25 | 04:28 | 10:49 | 5/7/8 | P270 | NA | NA | NA | 273 | 75 | 142.0 | 200.0 | 1200 | DI | 2.8 | 3.3 |
| 36..... | 1998 Jan 25 | 14:29 | 15:26 | 3/2/6 | N21E25 | C1.1 | 14:29 | 15:23 | 112 | 360 | 693.0 | 692.3 | 54 | DU | 213.7 | -7.4 |
| 37..... | 1998 Feb 2 | 17:49 | 18:27 | 5/3/4 | N25E74 | B7.7 | 17:31 | 17:55 | 72 | 55 | 501.8 | 501.8 | 24 | FL | 348.5 | 22.6 |
| 38..... | 1998 Feb 25 | 21:44 | 23:27 | 3/5/9 | NA | NA | NA | NA | 74 | 65 | 289.0 | 289.0 | 150 | DI | 32.1 | 1.3 |
| 39..... | 1998 Mar 22 | 07:03 | 07:41 | 2/5/2 | S30E70 | M1.1 | 06:51 | 07:00 | 104 | 49 | 416.9 | 416.9 | 9 | FL | 772.1 | -3.0 |
| 40..... | 1998 Mar 23 | 00:01 | 00:50 | 7/4/12 | P060 | NA | NA | NA | 94 | 84 | 357.8 | 500.0 | 49 | DI | 170.1 | -3.0 |
| 41..... | 1998 Mar 23 | 07:23 | 09:33 | 11/10/8 | NA | NA | NA | NA | 271 | 111 | 308.8 | 400.0 | 640 | DI | 10.4 | 9.2 |
| 42..... | 1998 Mar 27 | 00:47 | 01:23 | 7/3/6 | N30E41 | C1.0 | 00:36 | 00:46 | 88 | 87 | 568.1 | 568.1 | 10 | FL | 946.9 | 2.1 |
| 43..... | 1998 Apr 21 | 18:04 | 19:03 | 3/2/6 | P315 | NA | NA | NA | 292 | 62 | 527.0 | 526.0 | 126 | DI | 69.6 | 6.1 |
| 44..... | 1998 May 6 | 23:48 | 00:02 | 3/1/4 | S16W60 | M2.5 | 23:27 | 23:46 | 110 | 55 | 784.8 | 784.8 | 19 | FL | 688.4 | -9.7 |
| 45..... | 1998 May 8 | 01:36 | 02:28 | 3/3/6 | S16W83 | M3.1 | 01:49 | 02:04 | 287 | 76 | 371.0 | 600.0 | 15 | FL | 666.7 | -0.1 |
| 46..... | 1998 May 31 | 03:46 | 04:26 | 3/1/4 | P120 | C2.0 | 03:53 | 05:15 | 88 | 112 | 692.2 | 692.2 | 82 | FL | 140.7 | 8.7 |
| 47..... | 1998 Jun 2 | 07:54 | 08:08 | 4/2/3 | P225 | NA | NA | NA | 245 | 57 | 764.7 | 1150.0 | 285 | DI | 67.3 | 52.0 |
| 48..... | 1998 Jun 11 | 23:28 | 00:05 | 15/3/8 | P070 | C1.1 | 23:11 | 00:14 | 79 | 58 | 499.3 | 499.3 | 63 | DU | 132.1 | 2.8 |
| 49..... | 1998 Jun 11 | 09:01 | 10:28 | 9/1/6 | P070 | M1.4 | 09:57 | 10:27 | 123 | 177 | 830.1 | 830.1 | 30 | DU | 461.2 | -4.9 |
| 50..... | 1998 Jun 16 | 18:01 | 18:27 | 1/2/4 | P240 | M1.0 | 18:03 | 18:42 | 341 | 281 | 1481.7 | 1481.7 | 39 | FL | 633.2 | -74.6 |

[^2]CME Kinematic Evolution and Timing with Associated Flare


FIG. 1.-Schematic plot of CME kinematic evolution and its relation with temporal evolution of GOES soft X-ray flare. CME evolution may have three distinct phases: initiation phase, acceleration phase, and propagation phase, which correspond to the preflare phase, rise phase, and decay phase of the associated flare, respectively.
it emerges above the necessary occulter. The second effect is due to the angular-dependence of the electron Thomson scattering: the scattering is less efficient when an electron is further away from the plane of the sky (Vourlidas et al. 2000)

In Table 1 we list the observed properties of the 50 events selected in the order of observation date. The second and third columns show the first appearance times of CMEs in C1 and C2, respectively. The next column, which has three subitems, shows the number of times a CME was seen in $\mathrm{C} 1, \mathrm{C} 2$, and C 3 , respectively. Slower events should be seen in more images because it takes the CME a longer time to travel across the fields of view of the coronagraphs than a faster CME. The next column indicates the surface source region locations of CMEs, which are represented by heliographic longitude/ latitude coordinates if the source region is on the front side, and by position angle if the source region is not seen on the disk but above the limb. Five events that originated from the backside of the Sun are indicated by NA. The properties of the associated flares (if any) are shown in the next thee columns, which are for Geostationary Operational Environmental Satellite (GOES ) soft X-ray flare magnitude, start time, and peak time, respectively. The following three columns show the CME properties measured in C 2 and C 3 , which are for central position angle, angular width, and velocity (averaged across the C2 and C3 fields of view), respectively (adopted directly from the CDAW CME catalog). The next column shows the CME final velocity at the end of the main acceleration phase. Note that, for many of the 50 events, this velocity is close to the average velocity seen in C 2 and C 3 , and if this is the case, the
velocity is directly adopted from the previous column. However, for a number of events, the CME final velocity is very different from the average velocity in C2 and C3, especially for those events for which a significant portion of the main acceleration occurs in the C2 and C3 fields of view, e.g., gradual CME events with long and slow acceleration. The next column shows the duration of the main acceleration phase, which can be derived using two independent methods: a direct method and an indirect flare-proxy method; which method is used is indicated in the next column by "DI" (direct), "FL" (indirect, flare-proxy), or "DU" (dual methods) (see next section for a detailed explanation). The next column shows the magnitude of the main acceleration, which is the result of the CME final velocity divided by the acceleration duration. The residual acceleration of CMEs, which is the average acceleration seen in the C2 and C3 fields of view, is shown in the last column. The value is directly adopted from the CDAW CME catalog.

## 3. DETERMINING CME ACCELERATIONS AND RELATIONS WITH FLARES

### 3.1. Direct Method

The direct method is to simply interpret the CME velocity profile, directly derived from the measured height-time profile. This method works for those CMEs that have a sufficient number of C1 observations that the main acceleration phase of CME can be separated from the subsequent propagation phase. This normally requires at least three CME images seen in C1. Similar
studies, including several example events and their height-time and velocity-time plots, can be found in our previous works (Zhang et al. 2001, 2004). Instead of repeating the plots here, we summarize the observational properties in the sketch shown in Figure 1. This sketch is largely adopted from the velocity-time plot of the 1998 June 11 event published in Zhang et al. (2001). As indicated in the sketch, the full kinematic evolution of a CME undergoes three distinct phases: (1) an initiation phase, (2) an acceleration phase, and (3) a propagation phase. This scenario of CME kinematic evolution is also consistent with the observations of a much larger number of events investigated in this study. Simply put, phase 1 is characterized by a slow ascension of a largescale coronal structure (e.g., top envelope of an active region in the corona) for a period up to tens of minutes at a more or less constant speed of a few $\mathrm{km} \mathrm{s}^{-1}$ to tens of $\mathrm{km} \mathrm{s}^{-1}$. Phase 2, or the (main) acceleration phase, is characterized by a period of fast velocity increase, which lasts from a few minutes to tens of minutes (even longer for a few hours for more gradual events). Phase 1 and 2 take place mainly in the inner corona in the C 1 field of view. After the acceleration phase, a CME seems fully developed and propagates away with a more or less constant speed, a constant angular width and a constant position angle; hence, we simply call it the propagation phase. The main acceleration we are measuring refers to the rate of velocity change in phase 2 , while the residual acceleration refers to that in phase 3 .

Because of the nature of the multiple-phased evolution, it is essential to use piecewise fitting methods to derive the velocity and acceleration profiles from the height-time measurement. A piecewise fitting is to find velocity at a local time using two or three adjacent height-time points, equivalent to the first-order numeric derivative. Based on such obtained velocity profiles, we are able to track the velocity change point to point, and identify the onset and ending times, and hence the duration of the CME acceleration phase. The acceleration magnitude is simply the velocity increase during the acceleration phase divided by the acceleration duration. The uncertainty of the acceleration duration is simply determined by the observational cadences, which vary for C 1 , and are about 30 minutes for C 2 . For many of the events studied, the uncertainty of acceleration duration is about 30 min utes. The uncertainty of the calculated acceleration magnitude is largely inherited from the uncertainty of the duration. The uncertainty of velocity change should be relatively small, e.g., less than $10 \%$. As a result, the acceleration magnitude uncertainty is small for more gradual events, and large for more impulsive events. In this study, we limit ourselves to applying the direct method for more gradual events, e.g., those having acceleration duration longer than 30 minutes. Therefore, the uncertainty should be less than $50 \%$ for these events, and about $15 \%$ for those events whose acceleration duration is longer than 100 minutes. For more impulsive events, we use the indirect flare proxy method to determine the CME acceleration, described in the next subsection.

### 3.2. Indirect Method and Temporal Relationship Between CMEs and Flares

If a CME is associated with a GOES soft X-ray flare that occurs on the front disk, we are able to use the indirect flare-proxy method to obtain the two acceleration parameters, even if the acceleration is impulsive and there are only one or two CME images seen by C 1 . This method is based on the assumptions that (1) the rise time of the associated soft X-ray flare equals the CME acceleration time, and (2) the average velocity in the outer corona equals the velocity increase during the acceleration phase.


FIG. 2.-Comparison of CME acceleration duration (top panel) inferred from the direct method ( $Y$-axis) and the indirect flare-proxy method ( $X$-axis). The bottom panel shows the comparison of CME acceleration magnitudes. The solid diagonal lines indicate the equal values of the two methods.

These assumptions are justified by the observational fact that the CME acceleration phase usually coincides with the soft X-ray flare's rise phase, which was first demonstrated by Zhang et al. (2001). The sketch in Figure 1 also summarizes the temporal relationship between CME kinematic evolution and flare flux evolution. "Onset1 1 " in the figure indicates the start of the slow-rise initiation phase of CME, during which a small enhancement of soft X-ray flux might appear. "Onset 2" indicates the onset time of the main CME acceleration phase, which is also the onset time of the associated flare. The flare start time listed in the NOAA GOES flare catalog will correspond to the time at "onset 2 ," because it marks the fast rise of soft X-ray flux. Further, the main acceleration phase almost ends at the
peak of the soft X-ray flare. This kind of temporal coincidence between flare and CME, or CME-related-ejecta (e.g., filaments), has also been shown by many other studies (Gallagher et al. 2003; Shanmugaraju et al. 2003; Qiu et al. 2004; Maricic et al. 2004; Kundu et al. 2004; Sterling \& Moore 2005; Jing et al. 2005)

To further strengthen this point, we studied a subset of 10 events whose accelerations can be determined from both direct and indirect methods; these events are indicated by "DU" in column "TY" in Table 1. Figure 2 shows the comparison of the two accelerations. As shown in the top panel, the data points almost follow the straight diagonal line, indicating that the acceleration duration from the direct method is almost equal to that of the indirect method. The small deviation from the diagonal line is within the error bar, or the uncertainty associated with the direct method. This holds true for all events, ranging from extremely impulsive ones (e.g., event 1997 October 19, a few minutes acceleration) to extremely gradual ones (e.g., event 1996 October 5, 300 minutes of acceleration).

The acceleration magnitudes, shown in the bottom panel, also reveal the closeness of the values inferred from the two methods. Any deviation from the diagonal equal-line is within the error bar. Nevertheless, the uncertainty of acceleration magnitude from the direct method becomes larger for those strongly accelerated events, which are usually impulsive. Note that the extremely impulsive 1997 October 19 event is not plotted in the bottom panel, because its extremely large acceleration values are well beyond the plotting range. For this particular event, the acceleration duration is 6 minutes and the magnitude is $4464.9 \mathrm{~m} \mathrm{~s}^{-2}$ from the indirect method, while the duration is about 4.7 minutes and the magnitude is $7678.6 \mathrm{~m} \mathrm{~s}^{-2}$ from the direct method. This difference is also within the uncertainty associated with the direct method. For impulsive events, the acceleration parameters inferred from indirect method are probably more accurate than that from direct method.

In summary, out of the 50 events studied in this paper, the acceleration of 23 events, which are more gradual, are determined by the direct method only, while 17 events, which are more impulsive, are determined by the indirect flare-proxy method only. The accelerations of the remaining 10 events can be determined by both methods. For these dual events, we use the values determined from the indirect method for subsequent statistical analysis; the acceleration parameters listed in Table 1 are also from the indirect method.

## 4. RESULTS

### 4.1. Distributions of Main and Residual Accelerations

Figure 3 shows the distribution of the CME (main) acceleration and the residual acceleration for the 50 events studied. The $X$-axis denotes the event number as listed in Table 1. Note that the data point for event numbered 29 (1997 November 6) is omitted from the plot because of its exceptionally high value. The main acceleration spans the whole plotting range along the $Y$-axis, whereas the residual acceleration is limited to a very narrow range clustering around the solid horizontal line indicating zero acceleration. The statistical values about the distributions are listed in Table 2. For the 50 events, the median (average) value of the main acceleration is $170.1 \mathrm{~m} \mathrm{~s}^{-2}\left(330.9 \mathrm{~m} \mathrm{~s}^{-2}\right)$, while that of the residual acceleration is only $3.1 \mathrm{~m} \mathrm{~s}^{-2}\left(1.0 \mathrm{~m} \mathrm{~s}^{-2}\right)$. The standard deviation of the main acceleration is as large as $644.8 \mathrm{~m} \mathrm{~s}^{-2}$, while the standard deviation of the residual acceleration is only $25.3 \mathrm{~m} \mathrm{~s}^{-2}$. The maximum value of the main acceleration is $4464.9 \mathrm{~m} \mathrm{~s}^{-2}$, and the minimum value of the main acceleration is $2.8 \mathrm{~m} \mathrm{~s}^{-2}$. On the other hand, the maxi-


FIG. 3.-Distribution of CME main acceleration (plus signs) and residual acceleration (triangles) for the 50 events studied. The $X$-axis denotes the event number as listed in Table 1. The solid horizontal line indicates zero acceleration.
mum value for the residual acceleration is $52.0 \mathrm{~m} \mathrm{~s}^{-2}$, and the maximum negative value, which corresponds to deceleration, is $-131 \mathrm{~m} \mathrm{~s}^{-2}$.

In Figure 4 we show the histogram distribution of the same parameters. The extreme event of 1997 November 6 is also omitted from the plots for the sake of showing details for other events. The histogram plots demonstrate again that the main acceleration has a wide range, whereas the residual acceleration is limited to a small range centered around zero. One interesting fact is that the histogram of the main acceleration shows a single major peak at the lower end. The secondary peak at $700 \mathrm{~m} \mathrm{~s}^{-2}$ has only three events and may not be physically significant. Overall, there is no strong signature of a bimodal distribution of the acceleration. This implies that it is not appropriate to divide CME events into simply two classes (see discussion). For the residual acceleration, the distribution is centered around zero value, which is consistent with the view that CMEs display a largely constant speed in the outer corona.

In addition to the magnitude, another important parameter of (main) acceleration is the duration, whose distribution is shown in Figure 5. Like the magnitude, the duration also has a wide distribution, ranging from 6 minutes to about 1200 minutes. The median value is 54 minutes for the 50 events studied. The average value is 180 minutes. The histogram also shows a continuous distribution, with no sign of bimodal distribution. The implication of these observational results on CME classification will be discussed later.

### 4.2. A Scaling Law between Magnitude and Duration of Main Acceleration

One intriguing finding is that there is a strong inverse linear correlation between the acceleration magnitude and the acceleration duration as shown in Figure 6. This correlation is almost identical for the events measured by the direct method (triangles) and those events inferred from the indirect flare-proxy method ( plus signs). This kind of correlation has been reported earlier in a preliminary study based on a smaller sample of events

TABLE 2
Statistics of Main and Residual Accelerations

| Parameter | Main Accelleration |  | Residual Acceleration Magnitude ( $\mathrm{m} \mathrm{s}^{-2}$ ) |
| :---: | :---: | :---: | :---: |
|  | Duration (minutes) | $\begin{aligned} & \text { Magnitude } \\ & \left(\mathrm{m} \mathrm{~s}^{-2}\right) \end{aligned}$ |  |
| Median ...................... | 50.0 | 170.1 | 3.1 |
| Average ..................... | 180.0 | 330.9 | 0.9 |
| Standard deviation ...... | 285.9 | 644.8 | 25.3 |
| Minimum................... | 6.0 | 2.8 | -131.0 |
| Maximum.................. | 1200.0 | 4464.9 | 52.0 |




Fig. 4.-Histogram of the main acceleration (top panel) and the residual acceleration (bottom panel) for the 50 events studied.


Fig. 5.-Histogram of the acceleration duration during the main acceleration phase for the 50 events studied.
(Zhang 2005). The inverse correlation holds for the whole range of the acceleration parameters, which vary by more than 2 orders of magnitude. The relation can be described by a linear fit,

$$
\begin{equation*}
\log (A)=4.07-1.09 \log (T) \tag{1}
\end{equation*}
$$

where $A$ is the acceleration magnitude in unit of $\mathrm{m} \mathrm{s}^{-2}$ and $T$ is the acceleration duration in units of minutes. The correlation coefficient is -0.95 , indicating a strong correlation. Considering the uncertainty of measurement, we could round off the


Fig. 6.-Scattering plot of the magnitude vs. the duration of the CME main acceleration phase for the 50 events studied. There is a scaling law between the two acceleration parameters.


FIG. 7.-Scattering plots of CME velocity vs. acceleration magnitude (top panel), and CME velocity vs. acceleration duration (bottom panel). There is no apparent correlation between these parameters.
decimal points of the fitted parameters, which yields the simple expression

$$
\begin{equation*}
A=10,000 T^{-1} \tag{2}
\end{equation*}
$$

This formula reveals a scaling law of CME acceleration between the magnitude and the duration. More impulsive events tend to have stronger acceleration, whereas more gradual events tend to have weaker acceleration. When the formula is rewritten as $V=A T=10,000 \mathrm{~m} \mathrm{~s}^{-2}$ minutes, or $V=600 \mathrm{~km} \mathrm{~s}^{-1}$, it implies that on average all CME events will have the same final speed of $600 \mathrm{~km} \mathrm{~s}^{-1}$.

However, a CME's final velocity may vary from a few hundred to about $3000 \mathrm{~km} \mathrm{~s}^{-1}$ from event to event. The final speed of a CME is determined by the combination of two factors: the
acceleration magnitude and the acceleration duration; both are important in determining the final speed of a CME. To further clarify this point, we show the scattering plots between CME velocity and acceleration magnitude (Fig. 7, top panel), and between CME velocity and acceleration duration (Fig. 7, bottom panel ). There is no apparent correlation between CME velocity with either acceleration parameter. This implies that neither factor is dominant in determining the final velocity of a CME. It would be interesting to find out what physical mechanism(s) control the acceleration duration and what control the acceleration magnitude. However, this is beyond the scope of this paper.

## 5. DISCUSSION

### 5.1. The Issue of CME Classification

As shown above, the statistical distributions of CME acceleration, both magnitude and duration, show a continuous behavior. There is no strong sign of a bimodel distribution on acceleration. The earlier study on CME acceleration by St. Cyr et al. (1999) did not show this either. Further, the statistical distribution of CME velocity of thousands of events consistently showed a continuous distribution with a single peak (Howard et al. 1985; Hundhausen et al. 1994; St. Cyr et al. 2000; Yashiro et al. 2004; Yurchyshyn et al. 2005). Therefore, the parameters describing CME kinematic properties, including velocity, acceleration duration and acceleration magnitude, all show a continuous distribution.

In the literature a variety of events have been reported, ranging from extremely impulsive events to extremely gradual ones. St. Cyr et al. (1999) reported the largest acceleration among the 46 events they investigated to be $3270 \mathrm{~m} \mathrm{~s}^{-2}$. Zhang et al. (2001) reported a CME event with an acceleration as high as $7300 \mathrm{~m} \mathrm{~s}^{-2}$. Alexander et al. (2002) reported that a CME-associated X-ray ejecta had a peak acceleration of about $4800 \mathrm{~m} \mathrm{~s}^{-2}$, based on Yohkoh SXT observations. Gallagher et al. (2003) found a CMEassociated EUV ejection feature reaching a peak acceleration of about $1500 \mathrm{~m} \mathrm{~s}^{-2}$, based on Transition Region and Coronal Explore (TRACE ) observations. All these extremely impulsive eruptive events are associated with X class flares. MacQueen \& Fisher (1983) found that a number of events had fast but constant speed beyond a projected height of $0.2 R_{\odot}$ above the limb; these events must also be very impulsive because the acceleration took place within a very short distance. On the other hand, there are CMEs characterized by a very weak acceleration ( $<20 \mathrm{~m} \mathrm{~s}^{-2}$ ) over a long duration (several hours) and a long distance (e.g., up to $15 R_{\odot}$ ) (Sheeley 1999; Sheeley et al. 1999; Srivastava et al. 1999, 2000). These are extremely gradual CMEs. They do not show a phase of fast acceleration. These CMEs are often not associated with any flares.

Nevertheless, most CME events reside between the extremely impulsive ones and the extremely gradual ones, characterized by acceleration in the order of hundreds of $\mathrm{m} \mathrm{s}^{-2}$. Jing et al. (2005) found that the accelerations of erupting filaments are mainly in the range of $50-400 \mathrm{~m} \mathrm{~s}^{-2}$. Individual events with normal accelerations have been reported by many studies (Wood et al. 1999; Shanmugaraju et al. 2003; Qiu et al. 2004; Vršnak et al. 2004; Kundu et al. 2004; Sterling \& Moore 2005). Zhang et al. (2004) showed an event ( 2000 October 25) with an acceleration duration of about 160 minutes and a magnitude of about $131 \mathrm{~m} \mathrm{~s}^{-2}$. This moderate acceleration continued until the CME reached a height of about 7.0 $R_{\odot}$. Events with similar intermediate kinematic characteristics have been reported before (Plunkett et al. 2000; Yurchyshyn 2002).

The continuous distribution of CME kinematic properties is not consistent with the speculation that there may be two distinct classes of CMEs: impulsive CMEs and gradual CMEs (Sheeley et al. 1999; Andrews \& Howard 2001; Moon et al. 2002; Zhang et al. 2002). These studies are based on a small number of selected events or selective events. Statistical analysis by Yurchyshyn et al. (2005) showed that the speed distribution for accelerating and decelerating events in the LASCO C 2 and C3 fields of view are nearly identical and to a good approximation they can be fitting with a single lognormal distribution. Vršnak et al. (2005) found that flare-associated CMEs and nonflare CMEs showed quite similar characteristics in the LASCO C2 and C3 fields of view, contradicting the concept of two types. We believe that the usage of the impulsive and gradual types should be limited to the convenience of reference. They should not be regarded as specific classes that are physically distinct from other events, since they are part of a continuous distribution.

### 5.2. Implications on CME Modelings

Here we discuss the implications of our observational results, along with other relevant observations, on CME modelings. We consider the following three observational facts: (1) the wide and continuous distribution of CME acceleration in both magnitude and duration, and the scaling law of the acceleration; (2) the close temporal coupling between the CME bulk acceleration that occurs in macro scale and the flare particle acceleration that occurs in micro scale; and (3) the multiple-phase kinematic evolution of CMEs. A successful theoretical model should be able to explain these observational facts, regardless of its initial magnetic configuration, trigger process, and subsequent dynamic evolutions.

The temporal coincidence between CME acceleration and flare flux increase suggests that the run-away process of CME eruption is strongly coupled with the magnetic reconnection process that causes the flare. It has been widely accepted that a flare is caused by the magnetic reconnection process, which rapidly dissipates the magnetic energy prestored in the corona. Nonthermal energetic particles are accelerated inside or in the vicinity of the reconnection region through various possible mechanisms (e.g., see review by Priest \& Forbes 2002). When these energetic particles precipitate from the corona into the chromosphere along magnetic field lines, they spontaneously produce the hard X-ray emissions through the bremsstrahlungmechanism, and subsequently in an accumulation manner produce the soft X-ray emissions from the heated plasma evaporated from the chromospheric layer into the corona (e.g., Li et al. 1993). The evaporation process results in the well known "Neupert" effect between the soft X-ray profile and the hard X-ray profile of a flare: the time-derivative of the soft X-ray profile resembles the corresponding hard X-ray profile, especially during the soft X-ray flare's rise phase (Neupert 1968; Dennis \& Zarro 1993). Therefore, the rise phase of soft X-ray flare is believed to correspond to the main energy release phase in the corona through the magnetic reconnection. Further, it is found that, using filament eruption as a proxy, main CME acceleration occurs during the period of fast flare ribbon separation, a known signature of magnetic reconnection in the corona (Qiu et al. 2004; Jing et al. 2005). Qiu \& Yurchyshyn (2005) recently showed a good correlation between the reconnected magnetic flux and the final speed of CMEs. These observations suggest that the reconnection play an active role in CME acceleration. It is consistent with the traditional eruptive flare models, in which the driver is the magnetic reconnection underneath the rising prominence (Hirayama 1974; Kopp \& Pneuman 1976). The basic idea of the eruptive flare models is adopted by many CMEs models, in which
the magnetic reconnection occurs in the current sheet produced by the stretching of the erupting magnetic field, leading to the impulsive release of magnetic energy and the fast ejection of magnetic flux rope (Mikic \& Linker 1994; Lin \& Forbes 2000; Amari et al. 2000; Chen \& Shibata 2000; Moore et al. 2001; Cheng et al. 2003). In these models, the reconnection plays a role of fast tethercutting, which effectively disconnect the magnetic field lines from their foot points tied with the photosphere. In addition to the reconnection underneath the flux rope, the CME break-out models (Antiochos et al. 1999; MacNeice et al. 2004) also involve the magnetic reconnection above the escaping flux rope in a multipolar magnetic configuration.

The temporal coincidence also suggests that the CME run-away process and the magnetic reconnection process may mutually feed each other. The two processes not only start at the same time, but also end at almost the same time based on observations. The magnetic tether-cutting process is known to be very effective in accelerating the CME flux rope (Vršnak et al. 2004). First, it reduces the tension of the overlying restraining field by cutting the tie with the photosphere. Second, it increases the magnetic pressure below the flux rope by adding the poloidal flux through reconnection. Third, it enhances the outward hoop force due to the curvature of the flux rope thanks to the poloidal flux added. The escape of the flux rope reduces the magnetic pressure below, and thus induces an inflow toward the central current sheet; the current sheet is caused by the magnetic stretch as a result of the rising flux rope. Therefore, a faster rise of the flux rope causes a faster inflow, which results in a faster tether-cutting reconnection. At the same time, a faster reconnection causes a stronger outward force and thus a faster CME acceleration. The whole process, through flux rope rising, magnetic field stretching underneath, inflow tethercutting reconnection, and further accelerating, forms a closed loop of positive feeding, which leads to the simultaneous CME acceleration and flare energy release.

Another fact is that a CME may undergo multiple phases of kinematic evolution. Before the onset of the main acceleration (and also the onset of the flare), it is often observed that a CME (or a filament) undergoes a slow-rise phase (Kahler et al. 1988; Zhang et al. 2001; Maricic et al. 2004; Kundu et al. 2004; Schuck et al. 2004; Sterling \& Moore 2005), This phase is not trivial, because its rising speed is about $10-100 \mathrm{~km} \mathrm{~s}^{-1}$ and it may last for tens of minutes. This phase is certainly different from the nominal energy built-up phase driven by the photospheric movements, which, including the shearing motion, flux-cancellation, and fluxemergence, are all in the order of a few $\mathrm{km} \mathrm{s}^{-1}$, too small to account for the rising velocity. The magnitude of the rising velocity in the initiation phase indicates that the involved magnetic structure, possibly flux rope, has lost the quasi-static equilibrium. On the other hand, because of the lack of strong X-ray emission, there is no fast magnetic reconnection in this phase. The loss of the mechanic equilibrium has long been considered to be the trigger of the subsequent main energy release (Hirayama 1974). It is likely that the rising motion leads to the formation of the current sheet underneath, and the continuing rising motion stretches and strengthens the current sheet and eventually reaches the critical point that the fast magnetic reconnection sets in. Once the reconnection is triggered, the positive mutual feeding processes described above cause the rapid energy release and the eruption of the involved magnetic structure. Most computational CME models introduce a continuous shearing motion of the magnetic field in the photosphere to build up the free energy in the corona and drive the eruption of the system. These models usually show a transition from slow to fast motion of the erupting magnetic structure (Mikic \& Linker 1994; Lin \& Forbes 2000; Chen \& Shibata

2000; MacNeice et al. 2004). But, the transition in the models seems to be smooth, It is desirable to have models to demonstrate the distinct phases of CME kinematic evolution and review the transition mechanisms from phase to phase. There are at least four phases that a model should address: (1) the very slow energy build-up phase driven by the photospheric motion in the order of $1 \mathrm{~km} \mathrm{~s}^{-1}$, (2) a slow rise phase of certain erupting feature on the order of $10 \mathrm{~km} \mathrm{~s}^{-1}$, (3) a fast acceleration phase in the order of $100 \mathrm{~km} \mathrm{~s}^{-1}$, and (4) the near constant-speed propagation phase.

Finally, a robust theoretical model should explain the wide distribution of the kinematic properties of CMEs, including the distributions of the acceleration (from $\sim 10$ to $\sim 5000 \mathrm{~m} \mathrm{~s}^{-2}$, from $\sim 5$ to $\sim 1000$ minutes), the velocity (from $\sim 50$ to $\sim 3000 \mathrm{~km} \mathrm{~s}^{-1}$ ), and the size (from $\sim 10^{\circ}$ to $\sim 180^{\circ}$ ). Further, a good model should also explain the observed scaling law between the magnitude of the acceleration and the duration of the acceleration.

## 6. CONCLUSIONS

We have made a statistical study of the main and residual accelerations of CMEs. This is probably the first statistical study of the CME main acceleration in the inner corona. The obtained parameters shall enrich those parameters obtained before, including mass, size, velocity, and residual acceleration. We found that the two accelerations are indeed distinctly different. For the 50 events studied, the magnitude of the main acceleration ranges from 2.8 to $4464.0 \mathrm{~m} \mathrm{~s}^{-2}$, with a median (average) value of 170.1 ( $330.9 \mathrm{~m} \mathrm{~s}^{-2}$ ) and a standard deviation of $644.8 \mathrm{~m} \mathrm{~s}^{-2}$, whereas the magnitude of the residual acceleration ranges only from -131.0 to $52.0 \mathrm{~m} \mathrm{~s}^{-2}$ with a median (average) value of $3.1\left(0.9 \mathrm{~m} \mathrm{~s}^{-2}\right)$ and a standard deviation of only $25.3 \mathrm{~m} \mathrm{~s}^{-2}$. This result reinforces the view that there are distinct evolution phases of CMEs. We have further demonstrated that CME acceleration phase coincides with flare flux rise phase. Indeed, we have exploited this fact
and infer the CME acceleration duration using the rise time of associated flare. This indirect method is particularly useful for more impulsive events for which a direct measurement of acceleration is not possible. The duration of the main acceleration ranges from 6 to 1200 minutes, with a median (average) value of 54 ( 180 minutes) and a standard deviation of 286 minutes.

The CME main accelerations, in terms of both magnitude and duration, have a wide distribution that spans over almost 3 orders of magnitude. This wide distribution represents a continuous spectrum of CMEs events, ranging from extremely gradual ones all the way to the extremely impulsive ones. The histogram of CME accelerations shows a smooth profile with a single peak. The lack of bimodal distribution implies that it is not appropriate to classify CMEs into two simple classes, impulsive or gradual. We also find that the final velocity of a CME should be determined by the two acceleration factors: magnitude and duration. Neither factor is dominant in determining a CME's final speed. Finally, we find an interesting scaling law between the acceleration magnitude $(A)$ and the acceleration duration $(T)$ over the entire parameter range: $A\left(\mathrm{~m} \mathrm{~s}^{-2}\right)=10,000 T^{-1}$ (minutes). In logarithmic scale, the linear correlation coefficient is as high as 0.95 .
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[^1]:    ${ }^{2}$ See http://solar.scs.gmu.edu/research/cme_cl/inde.html.
    ${ }^{3}$ Available online at http://cdaw.gsfc.nasa.gov/CME_list; please refer to Yashiro et al. 2004 paper for a detailed description of the catalog.

[^2]:    ${ }^{\text {a }}$ The three subfields show the number of images a CME is seen in LASCO $\mathrm{C} 1, \mathrm{C} 2$, and C 3 , respectively.
    ${ }^{\mathrm{b}}$ The surface source region location of CMEs, represented by heliographic coordinate if on the front disk, and by position angle if from the limb.
    ${ }^{\text {c }}$ GOES X-ray flare magnitude. The next two columns are for the start time and the peak time of flares.
    ${ }^{\mathrm{d}}$ Position angle of CMEs, from NRL/GSFC/CUA CME catalog.
    e Angular width of CMEs, from NRL/GSFC/CUA CME catalog.
    ${ }^{\mathrm{f}}$ Propagation velocity of CMEs, from NRL/GSFC/CUA CME catalog.
    ${ }^{\mathrm{g}}$ Final velocity of CMEs. They are the same as the propagation velocity for most events, except those of gradual acceleration.
    ${ }^{h}$ The duration of the main acceleration.
    ${ }^{i}$ The method used in determining CME main acceleration.DI, FL, and DU indicate the direct method only, indirect flare-proxy method only, and dual methods, respectively.
    ${ }_{k}^{j}$ Magnitude of main acceleration.
    ${ }^{\mathrm{k}}$ Magnitude of residual acceleration, from NRL/GSFC/CUA CME catalog.

